

## ***Interactive comment on “A dynamical reconstruction of the Last Glacial Maximum ocean state constrained by global oxygen isotope data” by Charlotte Breitkreuz et al.***

### **Anonymous Referee #3**

Received and published: 18 June 2019

#### Summary

This paper applies the adjoint gradient method in an ocean general circulation model to the problem of ocean state estimation at the Last Glacial Maximum. The state estimate is constrained by upper-ocean temperature data and upper-ocean and benthic data for the oxygen isotope ratio of calcite. The inclusion of a new data type (planktonic foraminiferal oxygen isotopes) and new control variables (isotopic composition of precipitation and water vapor) make this paper a useful and novel contribution to the field. At this stage I am recommending major revisions because of some outstanding questions about the methodology and results, detailed further below.

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#### Major points

1. A key result that the authors have omitted is what the changes to the model controls look like. Are they consistent with possible atmospheric conditions at the LGM? In addition to giving the reader a sanity check (particularly for the isotopic controls, which are novel in this work), plotting the control adjustments can provide physical insights into how and why the model is fitting the data. Given that this configuration also adjusted ocean mixing, it would be interesting to see how fields of mixing parameters were changed to fit the data.

2. The authors apply two different normalizations and multiplicative factors to the computation of the control component of the cost function. While the proof is ultimately in the pudding – a solution was found – these factors (the  $N_{\text{data}}/N_{\text{ctrl}}$  term and the “preconditioning”) change the statistical interpretation of the cost function and the adjoint procedure. In particular, I suspect that the  $J'_{\text{ctrl}}$  term, which is an important indicator of whether the control adjustments have a reasonable amplitude relative to their a priori uncertainties, means something different under all of these scalings. I highly encourage the authors to simplify their description and put the various scalings into the control uncertainties, which is mathematically identical to what they have done already but more intuitive to the reader.

3. I wonder whether the experiments with adjoint sensitivities to AMOC would be better explored in more detail in a separate paper. Some of the challenges in making sense of sensitivities are illustrated by modern AMOC sensitivity studies of Pillar et al. 2016 and Kostov et al. 2019. Extending these sensitivities to decide which records are useful and which are not is potentially powerful, but should probably be approached with caution. Are these sensitivities large enough to be meaningful? Is the system linear enough that they apply under forcings similar to actual ocean variability? How can we use transient sensitivities to inform equilibrium sensitivity? How does this approach take into account that some regions are already relatively well sampled? See e.g. Comboul et al. 2014 for an application of sensor placement procedures to paleo problems.

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4. It would be useful to give some more information about the number of adjoint iterations you used and your criterion for solution convergence.

5. How unique is this solution likely to be?

6. It would be useful to provide more comparisons of the solution with other state estimates and to rationalize their differences.

Line-by-line comments

p119 Please give an age range for Late Holocene.

p1112-13 This statement could use clarification. What kinds of data? On what time scales?

p1116 today's

p1121 extent, not extend, though you could consider being more specific

p1118 Suggest "Some estimates are based only on... while others include the assimilations..."

p1121 It is not clear what "longest" means in this context

p316 Suggest "an indication of which... are most important to measure in order to constrain AMOC strength."

p412 Time anomalies

p3118 Please define time ranges you are targeting for LGM and LH

p4111 and elsewhere: I am not sure what CoP's policy is on citing work that has not been published. It would be helpful to see the manuscript of Breikreuz et al. 2019.

p519 What is the origin of the first-guess controls?

p5113-14 Please clarify this statement ("the longer the simulation, the more difficult...") Is it that it is difficult to reduce the cost function quickly? It would be helpful to provide

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an example or citation. I don't know that the Evensen paper deals with long time scales or adjoint methods.

p5119 Is there a contribution to  $d18O_w$  due to evaporation as well?

p613 By the isotopic control variables, do you mean the isotopic composition in precipitation and water vapor? It's confusing why eliminating a control variable would make the fit worse.

p614 I don't think you have established that it is non-convex(?) so suggest "non-convexities" rather than "the non-convex shape"

p617 Large changes compared to what?

p6111 Please state that these are the LGM-LH anomalies.

p7113-14 Including such a scale factor changes the interpretation of the cost function and the role of the control uncertainties. Taking a step back, if you assume that there is a model-data misfit and that the data uncertainties are correctly specified, if one finds that the controls are not being adjusted, the suggestion is that the prior control uncertainties are too small. Multiplying by this factor has the effect of increasing these uncertainties (the sigma in Table 3) by a factor of  $\sqrt{N_{ctrl}/N_{data}}$ .

I think it is useful and important to report the scaling this way to the reader (as inflated uncertainties) because it is a key control on how much the model can be changed to fit the data. In particular,  $J'_{ctrl}$  in Table 3 and elsewhere should be adjusted to the unscaled case, lest the impression be given that very small control changes sufficed to fit the data.

p815 "supports..." Can you clarify? The impression seems to be that including this term makes the solution equilibrated; is that the case?

p8Eq1 (mislabeled, not the first equation): Annual mean temperature where? surface ocean, all depths? What does it mean that there are drifts in annual mean sea surface

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elevation – is sea level changing? Is the variance in space meant instead? Also, please clarify what is meant by southward transport – net?

p8l7 Please elaborate on what is meant by “a sufficient reduction of the cost function” and describe more how these weights are derived.

p8l8 Please elaborate on this preconditioning. “Size” could be replaced by the clearer “amplitude” if that is in fact the meaning. Is this normalization in addition to that coming from the multiplication by the  $W$ s in the equation on page 7? If so, this additional preconditioning should also probably be included in the computation of  $J'_{ctrl}$  in Table 2.

p9l10 Please clarify why the model was run out in this repeating fashion. Was it a computational convenience? Does the model drift strongly?

p9l16 Strength at which depth level?

p10l6 A value below one can also point to the undesirable result of overfitting the observations. Is there any danger of that happening here with the value of  $J_{misfit}=0.7$  for SSTs? The posterior misfits appear to be quite small, though it's hard to tell because they have not been normalized by their uncertainties.

Figures 2 and 3: I would consider not whitening out misfits that are lower than uncertainty. It makes it look like the data are being overfit.

p10l7-8 “Only single. . .” I'm not sure what you meant by this.

p10l9 And in the North Atlantic subpolar gyre!

p10l10 I would avoid “greatly” and “small” or put in some values for comparison.

p10l14 Can you say more about what is meant by “locally big” and “implausible”?

p11l1 I don't think  $J'_{ctrl}$  represents global mean changes in individual control fields; rather, it's the sum of squared, /local/ changes normalized by uncertainties

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p11l4 Why is global mean sea surface elevation drifting – is there an imbalance in E-P-R? Also, is this temperature drift measure for the upper ocean? The entire ocean? It would be helpful to have some numbers to compare these to (e.g., modern interannual variability) so that the reader can assess the extent to which the model is driving.

p11l5 Can you be more specific than “the center of the AMOC”?

p11l17 Couldn't these high anomaly values also be due to the control adjustments?

Figure 4: Please say what the lower panel is.

p12l9 Please clarify what about the estimated AMOC is weaker

p12l12 Please clarify what is meant by “extent”

p12l11 I think there is room in this section to provide some more results and discussion if you would like to make the broad statement that the estimated LGM state ocean is similar to the modern (LH?). Or shift the focus of the statement to the Atlantic.

Section 3.3 It is important to emphasize that these are linear sensitivities. Also, what is the meaning of the sensitivities? Are these anomalies that are imposed for a certain time, at a certain lag? Please clarify in the text.

p13l1 Please restate what is meant by “the AMOC” – strength, structure, etc.

p14l1 This is a little confusing; it sounds like the Arctic and North Atlantic are affected by surface ocean changes.

p15l9-10 higher. . . smaller. . . Relative to LH? Please specify.

p15l14 extent, not extend

p16l1 This seems a bit chicken-and-egg to me.

p16l5 Can you discuss why the results might be dissimilar? Might it be due in part to the fact that the model is still spinning up?

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p16l10 The meaning of this section title is not clear.

p16l11 I would say instead that they do not require the presence of a shallower NADW.

p16l13 What is meant by single data points indicating a mismatch? Please clarify.

Fig. 10 Is MLD ever referenced in the text?

p17l2 Why not lower LH values?

p17 l9-10 Please be more specific than “the southern part”

p18l1-2 But are the misfits the same?

p18l6 The “southward transport” seems to be used as a measure of the separation between upper and lower cells. Please spell this out more clearly.

4.3 These sensitivities are for various transient lag times. How do they inform the equilibrium sensitivity, which seems to be relevant for the LGM problem?

p18l20 It would be useful to have a comparison with other LGM state estimates (Dail, etc.) and a discussion of why the results might be different.

p19l1 I think the authors should exercise greater caution in interpreting the adjoint sensitivities as observational placement experiments. For one, they ignore the locations where we already have observations. Second, they are linear (perturbation) sensitivities. It would be worth testing (using a set of perturbations of various sizes) whether the response to these patterns remains linear at amplitudes that we might expect to see in nature. See the examples of Pillar et al. 2016 and Kostov et al. 2019.

p19l12-13 Please provide a citation for this claim

p19l16 Confusing; please rephrase.

p19l23 What is meant by the extension of the cost function. . . Longer adjoint simulations?

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Interactive comment on Clim. Past Discuss., <https://doi.org/10.5194/cp-2019-52>, 2019.

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