Development and evaluation of a system of proxy data assimilation for paleoclimate reconstruction

By

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Abstract

Data assimilation (DA) has been successfully applied in the field of paleoclimatology to reconstruct past climate. However, data reconstructed from proxies have been assimilated, as opposed to the actual proxy values. This banned to fully utilize the information recorded in the proxies. This study examined the feasibility of proxy DA for paleoclimate reconstruction. Isotopic proxies (δ¹⁸O in ice cores, corals, and tree-ring cellulose) were assimilated into models: an isotope enabled general circulation model (GCM) and forward proxy models, using offline data assimilation.

First, we examined the feasibility using an observation system simulation experiment (OSSE). The analysis showed a significant improvement compared with the first guess in the reproducibility of isotope ratios in the proxies, as well as the temperature and precipitation fields, when only the isotopic information was assimilated. The accuracy for temperature and precipitation was especially high at low latitudes. This is due to the fact that isotopic proxies are strongly influenced by temperature and/or precipitation at low latitudes, which, in turn, are modulated by the El Niño-Southern Oscillation (ENSO) on interannual timescales. The proxy temperature DA had comparable or higher accuracy than the reconstructed temperature DA.

The proxy DA was compared with real proxy data. The reconstruction accuracy was decreased compared to the OSSE. In particular, the decrease was significant over the Indian Ocean, eastern Pacific, and the Atlantic Ocean where the reproducibility of the proxy model was lower. By changing the experimental design in a stepwise manner, the decrease in accuracy was found to be attributable to the misrepresentation of the models. In addition, the accuracy was also dependent on the number and/or distribution of the proxies to be assimilated. Thus, to improve climate DA, it is necessary to enhance the performance of models, as well as to increase the number of proxies.
1. Introduction

Knowledge of past conditions is crucial for understanding long-term climate variability. Historically, two approaches have been used to reconstruct paleoclimate; one based on the empirical evidence contained in proxy data, and the other based on simulation with physically-based climate models. Recently, an alternative approach combining proxy data and climate simulations using a data assimilation (DA) technique has emerged. DA has long been used for forecasting weather and is a well-established method. However, the DA algorithms used for weather forecasts cannot be directly applied to paleoclimate due to the different temporal resolution, spatial extent, and type of information contained within observation data (Widmann et al., 2010). The temporal resolution and spatial distribution of proxy data are significantly lower (seasonal at best) and sparser than the present-day observations used for weather forecasts, and the information we can get does not measure the direct states of climate (e.g., temperature, wind, pressure, etc.), but represents proxies of those states (e.g., tree-ring width, isotopic composition in ice sheets, etc.). Thus, DA applied to paleoclimate is only loosely linked to the methods used in the more mature field of weather forecasting, and it has been developed almost independently from them.

Several DA methods have been proposed for paleoclimate reconstruction (von Storch
et al., 2000; van der Schrier et al., 2005; Dirren and Hakim, 2005; Goosse et al., 2006; Bhend et al., 2012; Dubinkina and Goosse, 2013; Steiger et al., 2014), and paleoclimate studies using DA have successfully determined the mechanisms behind climate changes (Crespin et al., 2009; Goosse et al., 2010; 2012; Mathiot et al., 2013). In previous studies, the variables used for assimilation have been data reconstructed from proxies (e.g., surface air temperature) because observation operators or forward models for proxies have not been readily available. Hereafter, the DA method that assimilates reconstructed data from proxies is referred to as reconstructed DA. Recently, proxy modelers have developed and evaluated several forward models for stable water isotopic proxies (e.g., Dee et al., 2015 and references therein). In this study, we attempted to assimilate proxy data directly for the first time.

The main advantage of proxy DA over reconstructed DA is the richness of information used for assimilation. In previous studies, only a single reconstructed field was assimilated. However, proxies are influenced by multiple variables. Hence, the assimilation of a single variable does not use the full information recorded in the proxies. The reconstruction method itself also limits the amount of information. The most commonly-used climate reconstruction is an empirical and statistical method that relies on the relationships between climate variables and proxies observed in present-day
observations. These relationships are then applied to the past climate proxies to reconstruct climate prior to the instrumental period. Most of the studies using this approach assume that the relationship is linear. However, this assumption imposes considerable limitations in which specific climate proxies can be used, and proxies that do not satisfy the assumption have generally been omitted (e.g., PAGES 2k Consortium, 2013). Because information on paleoclimate is scarce, it is desirable to use as much information as possible.

Furthermore, the reconstruction method also limits the quality of information provided. The method also assumes stationarity of the relationship between the climate and the proxies. However, this assumption has been shown to be invalid for some cases (e.g., Schmidt et al. 2007; LeGrande and Schmidt, 2009). In the case of reconstructed DA, the assimilation of such erroneous data would provide unrealistic results. In the case of proxy DA; however, the accuracy of the assimilation is expected to be unchanged, provided the model can correctly simulate the non-stationarity.

The concept of proxy data assimilation is not new, and has been proposed in previous studies (Hughes and Ammann, 2009; Evans et al., 2013; Yoshimura et al., 2014; Dee et al., 2015). Yoshimura et al. (2014) demonstrated that the accuracy of the simulation results increased following assimilation of the stable water isotope ratios of vapor for...
current weather forecasting. They performed an observation system simulation experiment (OSSE) assuming that isotopic observations from satellites were available every six hours. Because the isotope ratio of water is one of the most frequently used climate proxies, this represents a significant first step toward improving the performance of proxy data assimilation in terms of identifying suitable variables for assimilation. However, it is not yet clear whether it is feasible to constrain climate only using isotopic proxies whose temporal resolution and spatial coverage are much longer and sparser than those of the specific study.

This study examined the feasibility of isotopic proxy DA for the paleoclimate reconstruction on the interannual timescale. Because the study represents the first attempt to assimilate isotopic variables on this timescale, we adopted the framework of an OSSE, as in previous climate data assimilations (Annan and Hargreaves, 2012; Bhend et al., 2012; Steiger et al., 2014). After the evaluation of proxy DA in the idealized way, we conducted the study with “real” proxy DA. We investigated which factors decreased or increased the accuracy of the proxy DA.

In this study, we used only oxygen isotopes ($^{18}$O) as proxies. The isotope ratio is expressed in delta notation ($\delta^{18}$O) relative to Vienna Standard Mean Ocean Water (VSMOW) throughout the manuscript. If the original data were expressed in delta
notation relative to Vienna Pee Dee Belemnite (VPDB), they were converted to the VSMOW scale.

This paper is structured as follows. In the following section, the data assimilation algorithm, models, data, and experimental design are presented. Section 3 shows the results of the idealized experiment. Section 4 gives the results of the real proxy DA. The Discussion is presented in Section 5. Finally, we present our conclusions in Section 6.

2. Materials and methods

2.1. Data assimilation algorithm

We used the so-called “offline data assimilation” algorithm to assimilate time-averaged data. In offline data assimilation, the analysis procedure is not cycled to the simulation (Bhend et al., 2012); thus, the background ensembles can be constructed from existing climate model simulations (Huntley and Hakim, 2010; Steiger et al., 2014). As such, we can assimilate data with any temporal resolution coarser than the model outputs. In this study, we focused on annual data assimilation. Following the procedure proposed by Steiger et al. (2014), the background ensemble was taken from part of a single climate model simulation, where the ensemble members were individual years instead of independent model simulations. This algorithm was selected to reduce computational
costs. This simplification was valid because the interannual variability in a single run was inherently indistinguishable from the variability in the annual mean within the ensemble of simulations in which the initial conditions were perturbed. Thus, the background ensembles were the same for all of the reconstruction years and did not contain any year-specific boundary conditions and forcing information; hence, the background error covariance was constant over time. Therefore, this study did not consider non-stationarity between the proxies and climate. Despite the limitations of the algorithm used in this study, it should be noted that the proxy DA could address non-stationarity by changing the algorithm. We return to this point in Section 5.

To control spurious long-distance correlations due to sampling errors, a localization function proposed by Gaspari and Cohn (1999) with a scale of 12,000 km was used. The detailed procedure used for the algorithm is described in Steiger et al. (2014).

2.2. Models

Isotope ratios recorded in ice cores, corals, and tree-ring cellulose were assimilated. To assimilate these variables, forward models for the variables are required. We used the forward model developed by Liu et al. (2013; 2014) for corals, and Roden et al. (2000) for tree-ring cellulose. We assumed that the isotopic composition of ice cores was the
same as that of precipitation at the time of deposition. Note that, in reality, the isotope ratio recorded in ice cores is not always equal to that in precipitation due to post-depositional processes (e.g., Schotterer et al., 2004). Because detailed models that explicitly simulate the impact of all the processes involved in determining the value of the ratio are not yet available, we used the isotope ratio in precipitation for that in ice cores to avoid adding unnecessary noise.

The isotopic composition in precipitation was simulated using an atmospheric general circulation model (GCM) into which the isotopic composition of vapor, cloud water, and cloud ice are incorporated as prognostic variables. The model explicitly simulates the isotopic composition with all the details of the fractionation processes combined with atmospheric dynamics and thermodynamics, and hydrological cycles. Hence, the model simulates the isotopic composition consistent with the modeled climate. Although many such models have been developed previously (Joussaume et al., 1984, Jouzel et al., 1987; Hoffmann et al., 1998; Noone and Simmonds, 2002; Schmidt et al., 2005; Lee et al., 2007; Yoshimura et al., 2008; Risi et al., 2010; Werner et al., 2011), we used a newly-developed model (Okazaki et al., in prep.) based on MIROC5 (Watanabe et al. 2010). The spatial resolution was set to T42 (approximately 280 km) with 40 vertical layers.

The variability in $\delta^{18}O$ recorded in coral skeleton aragonite ($\delta^{18}O_{\text{coral}}$) depends on
calcification temperature and local $\delta^{18}$O in sea water ($\delta^{18}$O$_{sw}$) at the time of growth (Epstein and Mayeda, 1953). Previous studies have modeled $\delta^{18}$O$_{coral}$ as the linear combination of sea surface temperature (SST) and $\delta^{18}$O$_{sw}$ (e.g., Julliet-Leclerc and Schmidt, 2001; Brown et al., 2006; Thompson et al., 2011), as follows:

$$\delta^{18}O_{coral} = \delta^{18}O_{sw} + aSST$$

where $a$ is a constant which represents the slope between $\delta^{18}$O$_{coral}$ and SST. In this study, the constant was uniformly set to -0.22‰/°C for all the corals, following Thompson et al. (2011), and we used a model developed by Liu et al. (2013; 2014) to predict $\delta^{18}$O$_{sw}$. The model is an isotopic mass balance model that considers evaporation, precipitation, and mixing with deep ocean water. The coral model uses the monthly output of the isotope-enabled GCM as its input, except for the isotope ratio of deep ocean water, which was obtained from observation-based gridded data compiled by LeGrande and Schmidt et al. (2006). After the model calculates the monthly $\delta^{18}$O$_{coral}$, it is arithmetically averaged to provide the annual $\delta^{18}$O$_{coral}$.

The isotope ratio in tree-ring cellulose ($\delta^{18}$O$_{tree}$) was calculated using a model developed by Roden et al. (2000). In this model, $\delta^{18}$O$_{tree}$ is determined by the isotopic composition of the source water used by trees for photosynthesis, and evaporative enrichment on leaves via transpiration. In this study, the value of the isotopic composition
in the source water was arbitrarily assumed to be the moving average, traced three-months backward, of the isotopic composition in precipitation at the site. Again, the model used the monthly output of the isotope-enabled GCM as its input. After performing the tree-ring model calculation, the monthly output was weighted using climatological net primary production (NPP) to calculate the annual average. The NPP data were obtained from the US National Aeronautics and Space Administration (NASA) Earth Observation website (http://neo.sci.gsfc.nasa.gov).

Because the isotopic compositions of the proxies were simulated using the output of the isotope-enabled GCM, their horizontal resolution was the same as that of the GCM.

2.3. Experimental design

2.3.1. Control experiment

The first experiment served as a control (CTRL) experiment, and used the framework of an OSSE. In the experiment, the “simulation” and the “truth” (nature run) were simulated by the same models, with the same forcing, but with different initial conditions. Because the proxy models were driven by the output of the GCM, the modeled proxies were consistent with the modeled climate from the GCM. Thus, here we describe the experimental design for the GCM. The GCM was driven by observed SST and sea-ice data (HadISST; Rayner et al., 2003), and historical anthropogenic (carbon dioxide,
methane, and ozone) and natural (total solar irradiance) forcing factors. The simulation covered the period of 1871–2007 (137 years).

Although the simulation period included recent times covered by observational data, we assumed that the only variable that could be obtained was the annual mean of $\delta^{18}O$ in the proxies. We based this assumption on the fact that we wished to perform the DA for a period in which no direct measurements were available, and there were only climate proxies covering the period. Therefore, the temporal resolutions of the “observations” and “simulations” were also annual, considering the typical temporal resolution of the proxies.

Observations were generated by adding Gaussian noise to the truth. The spatial distribution of the observations mimicked that of the proxies. The spatial distributions of each proxy for various periods are mapped in Figure 1. As can be seen from the figure, the distributions and the number of proxies varied with time. However, for the sake of simplicity, the distributions of the proxies were assumed to be constant over time in the CTRL experiment (Figure 1 a). The size of the observation errors will be discussed in Section 2.4.

The state vector consisted of five variables; surface air temperature and amount of precipitation, as well as the isotopic composition in precipitation, coral, and tree-ring cellulose. The first three variables were obtained from the isotope-enabled GCM, and the
other two variables were obtained from the proxy models driven by the output of the
GCM.

2.3.2. Real proxy data assimilation

The second (REAL) experiment assimilated proxy data sampled in the real world. To mimic realistic conditions, SST and sea-ice concentration data to be used as model forcing were modified from observational to modeled data. In reality, there were no direct observations available for the target period of the proxy DA. Therefore, to reliably evaluate the feasibility of proxy DA, the first estimate should be constructed using modeled SST, as opposed to observed SST. We used SST data from the historical run of the Coupled Model Intercomparison Project Phase 5 (CMIP5; Taylor et al., 2007) from the atmosphere-ocean coupled version of MIROC5 (Watanabe et al., 2010) obtained from the CMIP5 data server (https://pcmdi.llnl.gov/search/cmip5/).

Because the experiment was not an OSSE, nature run was not necessary.

2.3.3. Sensitivity experiments

Four sensitivity experiments were conducted to test the robustness of the results of the proxy DA. In the first sensitivity experiment (CGCM), the simulation run was
constructed from the simulation forced by the modeled SST and sea ice as in the REAL experiment. The other settings for the simulation run were the same as those in the CTRL experiment. The nature run was the same as that of the CTRL experiment. Thus, this experiment investigated how the accuracy of the results was decreased by using the simulated SST.

In the second sensitivity experiment (VOBS), the experimental design was the same as that in the CGCM, except for the number of proxies that were assimilated. In the CGCM experiment, the distribution and number of proxies were set to be constant over time, as in the CTRL experiment. In the VOBS experiment, the distribution and number of proxies varied with time to reliably evaluate the results of the REAL experiment relative to those from the CTRL experiment.

In the third sensitivity experiment (T2-Assim), the surface temperature added with Gaussian noise was assimilated. The purpose of the experiment was to compare the accuracy of the reconstructed DA with that of the proxy DA. The experimental design was the same as that in the CTRL experiment, except for the variables that were assimilated. The noise was added to consider the uncertainties stemmed from the reconstruction. The size of error was determined by considering the typical signal-to-noise ratio (SNR) values of 0.25 and 0.50 (Mann et al., 2007), as well as a further value.
The final sensitivity (M08) experiment was used to examine the sensitivity to the observation network. The experimental design was the same as for the CTRL, except for the spatial distribution of the proxy. The proxy network used in the experiment was the same as that of Mann et al. (2008). We assumed that isotopic information was available for all the sites, even when this was not the case. For example, even if only tree-ring width data were available at some of the sites in Mann et al. (2008), in this experiment we assumed that isotopic data recorded in tree-ring cellulose were available at the site. The number of grids containing observations were 108 and 250 for the CTRL experiment and M08 respectively.

The experimental designs are summarized in Table 1.

2.4. Observation data

We used paleoclimate data archived at the National Oceanic and Atmospheric Administration (NOAA; https://www.ncdc.noaa.gov/data-access/paleoclimatology-data) and data used in the PAGES 2k Consortium (2013). Additionally, 22 tree-ring cellulose and 7 ice core data sets were collected separately from published papers. We only used oxygen isotopic data ($^{18}$O) whose temporal resolution was higher than annual; proxies
whose resolution was lower than annual were excluded. The full list of proxies used in this study is given in the Appendix. Following Crespin et al. (2009) and Goosse et al. (2010), all proxy records were first normalized, and then averaged onto a T42 grid box to eliminate model bias and produce a regional grid box composite. To compare the results from each experiment effectively, the assimilated variables were all normalized in both the simulation and nature runs, and in the observations in all the experiments.

Errors were added to the truth in a normalized manner to provide the observation. The normalized error was uniformly set to 0.50 for all proxies. This was based on the measurement error of δ¹⁸O in ice cores being reported to range from 0.05 to 0.2‰ (e.g., Rhodes et al., 2012; Takeuchi et al., 2014), and the corresponding normalized error (measurement error divided by standard deviation of proxy) then ranges from 0.03 to 0.1, with an average of 0.06. Similarly, the measurement error of δ¹⁸O in coral ranges from 0.03 to 0.11‰ (e.g., Asami et al., 2004; Goodkin et al., 2008), and the corresponding normalized error ranges from 0.24 to 1.1, with an average of 0.53. The measurement error of δ¹⁸O in tree-ring cellulose ranges from 0.1 to 0.3‰ (e.g., Managave et al., 2011; Young et al., 2015), and the corresponding normalized error ranges from 0.08 to 0.55, with an average of 0.28. In practice, due to the error of representativeness and that in observation operator, it is common to increase the observation errors to ensure that the analysis
functions effectively (Yoshimura et al., 2014). Furthermore, the measurement errors were not always available; therefore, a uniform value of 0.5 was used for all the proxies.

3. Results from the OSSE

The time series of the first estimation, the analysis, and the real values for $\delta^{18}O$ in corals are compared as an example in Figure 2 at a location where observational data were available (1°N, 157°W). Because the first estimate was the same for all reconstruction years, it is drawn as horizontal lines. After the assimilation, the analysis agreed well with the real values ($R = 0.96, p < 0.001$). This confirmed that the assimilation performed well.

We then examined how accurately the other variables were reconstructed by assimilating isotopic information. Figure 2 also shows the time series of surface air temperature and precipitation for the same site. There was a clear agreement between the analysis and the truth for both variables ($R = 0.92$ and 0.88 respectively for temperature and precipitation).

This indicated that temperature and precipitation were effectively reconstructed by assimilating isotopic variables at this site. This was because the isotope ratio in corals has a signature not only from temperature as given in Eq. 1, but also precipitation (Liu et al., 2013); the correlation with $\delta^{18}O_{\text{coral}}$ was -0.88 ($p < 0.001$) for both temperature and precipitation, respectively. This example shows that the isotopic proxy records more than
one variable.

Figure 3 maps the correlation coefficients between the analysis and the truth for the isotope ratio, temperature, and precipitation for 1970–1999. Because the first estimate was constant over time, the temporal correlation between the first estimate and the real value was zero everywhere. Thus, a positive correlation indicated that the DA improved the simulation.

The correlation for $\delta^{18}O$ in precipitation were high at the observation sites, regardless of the proxy type. This was because $\delta^{18}O$ in both corals and trees is affected by the isotopic composition in precipitated water derived from sea water or soil water. The correlation for $\delta^{18}O$ in tree-ring cellulose were also high at the observation sites. On the other hand, the correlation for $\delta^{18}O$ in corals were generally high at low- to mid-latitudes, and the spatial pattern was similar to that of surface temperature. In contrast, closely correlated areas were restricted to low-latitude for precipitation.

How can the spatial distribution of the correlation pattern be explained; i.e., what do the proxies represent? To investigate this question, empirical orthogonal function (EOF) analysis was conducted for the simulated $\delta^{18}O$ in precipitation, corals, and tree-ring cellulose. Only grids that contained observations were included in the analysis. The variables were centered around their means before the analysis. The data covered the
period 1871–2007. The EOF patterns and temporal correlations between surface
temperature and the characteristic evolution of EOF, or the principal components (PCs)
of the first mode of each proxy are shown in Figure 4.

The first mode of $\delta^{18}O$ in ice core explains 14.3% of the total variance and it is the
only significant mode according to the Rule of Thumb (North et al., 1982) (the first and
the second mode were indistinguishable). The maximum loadings were in Greenland and
Antarctica where temperature has been increasing significantly for the past hundred years.
Indeed, the PC1 shows the significant trend and is correlated with global mean surface
temperature ($R=0.44$, $p < 0.001$). Therefore, it is legitimate to regard ice core data as a
proxy of global temperature as revealed from observation (Schneider and Noone, 2007).

The first modes of $\delta^{18}O$ in corals, and tree-ring cellulose represent ENSO. The
explained variance of the first modes of $\delta^{18}O$ in corals, and tree-ring cellulose was 44.2,
and 19.0%, respectively. The maximum loadings occurred in the central Pacific for corals,
and Tibet for tree-ring cellulose. The temporal correlation between the PC1s and NINO3
index were 0.95, and 0.37 for corals and tree-ring cellulose, respectively. Because the
isotopic composition in corals is influenced by sea temperature, it is expected that the
$\delta^{18}O$ in corals from the central Pacific records the ENSO signature. Interestingly, the
analysis revealed that the $\delta^{18}O$ in tree-ring cellulose was also influenced by ENSO; hence,
this proxy contributes to the reconstruction of temperature and precipitation over the tropical Pacific. Indeed, many previous studies have reported the link between δ¹⁸O in tree-ring cellulose and ENSO (Sano et al. 2012; Xu et al. 2011; 2013; 2015). The link was explained as follows by Xu et al. (2011): Numerous studies have associated Indian monsoon rainfall with ENSO (e.g., Rasmusson and Carpenter 1983), albeit the relationship was found to be non-stationary over time (Kumar, 1999). The positive phase of ENSO results in a decrease in summer monsoon rainfall in India, which leads to dry conditions in summer. The decrease in precipitation leads to isotopically-enriched precipitation, and the dry conditions enhance the enrichment of water in leaves. Correspondingly, the δ¹⁸O in tree-ring cellulose becomes heavier than normal in the positive phase of ENSO. Due to the relationships between the coral and tree-ring cellulose data and ENSO, the correlation coefficient between the analysis and real values for the NINO3 index was as high as 0.95 (p < 0.001).

Although EOF analysis did not reveal any other significant correlation between PCs and climate indices, climate indices for the North Atlantic Oscillation and Southern Annular Mode calculated using the reconstructed data were significantly correlated with the truth (0.59 and 0.46, respectively).
4. Real proxy data assimilation

Based on the results of the idealized experiment described in the previous section, we performed a “real” proxy DA, in which sampled and measured data in the real world were assimilated.

The temporal correlation between the analysis and observations for temperature and precipitation are shown in Figure 5 (d, h). The observations were obtained from HadCRUT3 (Brohan et al., 2006) for temperature, and GHCN-Monthly Version 3 (Peterson and Vose, 1997).

Although the real proxy DA had reasonable accuracy, it was inferior relative to the CTRL experiment. We investigated the cause of the decreased accuracy using the outputs of the sensitivity experiments. The design of the experiments was changed in a stepwise fashion to more realistic conditions of proxy data assimilation from the idealized conditions. The correlations between the analysis and the truth, or the observation, for the experiments are shown in Figure 5. The truths for the CGCM and VOBS experiments were the same as those for the CTRL experiment. The global mean correlation coefficients for temperature and precipitation in the experiments are summarized in Figure 6. Note that the correlation was averaged in the same domain for all the experiments to take into account the differences in representativeness.
In the CGCM experiment, the temporal correlations between the analysis and the real values were similar to those in the CTRL experiment for both temperature and precipitation (Figure 5 b, f). This indicates that ENSO and its impacts were well represented in the modeled SST used to construct the “simulation”. Watanabe et al. (2010) reported similar modeled SST and observational values for the amplitude of ENSO measured by the NINO3 index, and the spatial patterns of the temperature and precipitation fields regressed on the NINO3 time series (see Figures 13 and 14 in their report).

Because the number of proxies for assimilation differed from that in the CGCM experiment, it was not straightforward to compare the results of the REAL experiment with those of the CGCM experiment. To enable an effective comparison of the results, the same number of proxies were assimilated in the VOBS experiment as in the REAL experiment and the same settings were used as in the CGCM experiment for the other variables. Consequently, the performance of the assimilation of the VOBS experiment was similar to that of the CGCM experiment for 1970–1999. Because the number of proxies for assimilation was similar for this period, the assimilation of the VOBS experiment performed well.

When the REAL and VOBS experiments were compared, the correlation coefficients
for temperature were significantly decreased over the Indian Ocean, eastern Pacific, and Atlantic Ocean. These areas corresponded to areas of low reproducibility in the coral model (Liu et al, 2014). The effects of sea current and river flow in these areas, which were not included in the coral model, were deemed to be considerable. The reproducibility of δ¹⁸O in corals in these areas requires improvement to enhance the performance of the assimilation.

5. Discussion

5.1. Comparison with the reconstructed temperature assimilation

Hughes and Ammann (2009) recommended assimilating measured proxy data, as opposed to reconstructed data derived from the proxy data. This subsection compares the results from the CTRL and T2-Assim experiments with three different SNR values. Both experimental frameworks were OSSE, and the observations and reconstructed temperature were assumed to be available for the same sites as in the CTRL experiment. To account for the uncertainty derived from the statistical reconstruction, Gaussian noise was added to the temperature from the nature run to generate the observational values in the T2-Assim experiment in a similar fashion to the CTRL experiment. The SNR of the reconstructed temperature was set to 0.25 and 0.50, which are typical values for proxy
432 records (e.g., Mann et al., 2007). Additionally, we also considered an SNR value of 1.0.

Figure 7 shows the spatial distribution of the correlation coefficients for temperature and precipitation between the truth and the analysis for each experiment. The global mean correlation coefficients for temperature (precipitation) were 0.49 (0.29), 0.50 (0.22), 0.39 (0.16), and 0.25 (0.10) for the experiments assimilating $\delta^{18}$O in proxies, and those assimilating temperature with SNR values of 1.0, 0.50, and 0.25, respectively (Figure 8). The values were higher for the assimilated $\delta^{18}$O in proxy than for assimilated temperature, with SNR values of 0.25 and 0.50 for both precipitation and temperature. The temperature was reconstructed slightly accurately by assimilation of temperature with a low noise value (SNR = 1.0) than by assimilation of $\delta^{18}$O in the proxies. Although using an SNR = 1.0 produced more accurate reconstructed field than the ordinal statistical reconstruction, the superior accuracy of the assimilation of proxy data relative to the assimilation of reconstructed temperature was dependent on the magnitude of the SNR; i.e., the accuracy of assimilation of the reconstructed values was dependent on the quality of the reconstructed data. The quality of the reconstructed data was in turn dependent on the stationarity between the proxies and climate, and the degree to which the proxy was affected by factors other than the variable of interest. Isotope-enabled GCMs (Schmidt et al. 2007; LeGrande and Schmidt. 2009) and observations and models for tree-rings
(D’Arrigo et al. 2008; Evans et al. 2014) have demonstrated non-stationarity and non-linearity between proxies and climate. Thus, we cannot expect that a high SNR will be maintained over time. However, stationarity and linearity do not have to be considered if the forward proxy model is well-defined (Hughes and Ammann, 2009). Therefore, the assimilation of proxy data offers a useful tool for the reconstruction of paleoclimate, in which the relationship between the proxies and climate constructed with the present-day conditions does not apply.

5.2. Sensitivity to the distribution of the proxies

The accuracy of the proxy DA was relatively low over Eurasia and North America, even in the idealized experiment. It was unclear whether this was because of limitations in the proxy data assimilation or the scant distribution of the proxies. This subsection investigates the reasons for the relatively low reproducibility in these areas by comparing the results of the CTRL and M08 experiments, focusing on North America. The number of grids for which proxy data were available over North America was 11 and 126 for the CTRL and M08, respectively.

The results for North America are shown in Figure 9. The figure shows the temporal correlation coefficients between the analysis and the truth for surface air temperature and
precipitation. The correlation coefficients were calculated for 1970–1999. The accuracy was high in the area in which the proxies were densely distributed for both variables. The values of the coefficients averaged over the United States (30–50°N, 80–120°W) were 0.68 and 0.52 for temperature and precipitation, respectively. Compared to the CTRL experiment, the accuracy was enhanced for both variables. The values of the coefficients were 0.17 and 0.24, respectively, in the CTRL experiment. This implies that the performance of the reconstruction was strongly dependent on the distribution of the proxy data. Taking into consideration that proxy DA can assimilate not only proxy data, but also reconstructed data, proxy DA can take advantage of the use of increasingly large amounts of data. Although it is beyond the scope of this study, the combined use of these data is expected to improve the performance of proxy DA.

6. Conclusion

The feasibility of using proxy DA for paleoclimate reconstruction was examined in both idealized and real conditions experiments. The idealized (CTRL) experiment had high accuracy at low latitudes due to the dependency of coral data on temperature and precipitation in these regions, and the correlation between ENSO and δ¹⁸O in corals in Pacific and tree-ring cellulose in Tibet. We performed additional experiments to examine
the robustness of proxy DA. In the first experiment, the simulation run was constructed from a simulation forced by modeled SST and sea ice (CGCM experiment). The experiment examined the extent to which the accuracy of the results was decreased using the simulated forcings. The results showed little difference between the performance of the reconstruction for both the temperature and precipitation fields. This was because ENSO, which is the most important mode for the reconstruction, was well represented in the modeled SST. Finally, real proxy DA was performed, where the simulation run was constructed from the simulation forced by the modeled SST, and the real (observed) proxy data were assimilated into the simulation (REAL experiment). The accuracy of the reconstruction decreased over the Indian Ocean, eastern Pacific, and the Atlantic Ocean, where the reproducibility of the proxy model was lower.

The results indicated the need to improve isotope-enabled atmospheric GCM and proxy models. The differences between the CTRL and CGCM experiments were due to the use of misrepresented SST values by the coupled GCM. The differences between the CGCM and VOBS experiments were due to the large number of observations for assimilation. Finally, the differences between the VOBS and REAL experiments were due to the misrepresentation of the atmospheric GCM incorporating isotope and proxy models. The differences were largest between the VOBS and REAL experiments (Figure 6).
Although it is difficult at this stage to conclude which model caused the decrease in accuracy, it is necessary to improve the reproducibility of models in these regions, and we will investigate the reproducibility of each model in future studies. Furthermore, accurate models for ice cores that incorporate the entire post-deposition processes should be developed to enable more efficient utilization of all of the data.

In addition to model reproducibility, the proxy data may have contributed to the decrease in the accuracy of the proxy DA results by transferring erroneous values. It is possible that the data might not have been representative of the targeted temporal and/or spatial scales. Furthermore, it is also possible that the data were highly distorted by non-climatic factor(s). Thus, a thorough quality control, similar to the procedures used in weather forecasting, should be conducted before assimilation.

Although the accuracy of the REAL experiment was decreased compared with the CTRL experiment, it may still be possible to reliably reconstruct ENSO and ENSO-related variations in temperature and precipitation with this proxy network because the correlation coefficient between the analysis and the observations was as high as 0.83 in the REAL experiment. Although the reconstruction of ENSO is dependent on data from corals, and the time span covered by corals is relatively short (a few hundred years), ENSO can still be reliably reconstructed due to its global impact, as was demonstrated in
the relationship between isotopes in tree-ring cellulose from Tibet.

Moreover, because the reproducibility was heavily dependent on the spatial distribution, we expect that it will increase as more proxy data become available. In this sense, because proxy DA can assimilate both proxy and reconstructed data, the combined use of the two types of data is expected to improve the performance of the assimilation.

The DA algorithm used in this study did not consider non-stationarity among proxies and climate variables because the Kalman gain was constant over time. To address non-stationarity, the Kalman gain for a specific reconstruction year should be constructed for several tens of years before and after that year. Furthermore, an ensemble Kalman filter (EnKF) can only capture linear relationships between observations and the modeled state.

The use of other algorithms should be investigated in future studies for scenarios where non-linearity is not negligible. Thus, it is important in future studies to investigate non-stationarity and non-linearity among proxies and climate variables to identify suitable algorithms for proxy DA.

7. Acknowledgements

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Environment, and the CREST program of the Japan Science and Technology Agency.

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8. References


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Table 1. Experimental designs. The observation network used in the CTRL experiment is denoted as Orig.

<table>
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<th></th>
<th>SST data to drive simulation run</th>
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Spatial distribution of proxies (δ^{18}O in ice cores, corals, and tree-ring cellulose, denoted by blue, pink, and green, respectively). (a) Proxies spanning at least one year during 1871–2000 are mapped (b) The number of proxies is depicted as a function of time. (c–h)
h) The spatial distributions of the proxies are mapped for (c) 1871, (d) 1900, (e) 1930, (f) 1960, (g) 1990, and (h) 2007.
Figure 2
Annual mean δ¹⁸O in corals at a location where observational data were available (1°N, 157°W) for (a) background and (b) analysis. The black line indicates the truth, gray lines indicate ensemble members, and green line indicates the ensemble mean.
**Figure 3**

Temporal correlation between the analysis and the truth. The green dot represents the location of the proxy sampling site. The hatched area indicates where the correlation is not statistically significant ($p > 0.05$).
Figure 4
First mode of EOF and the correlation between PC1 and temperature for (a and d) ice cores, (b and e) corals, and (c and f) tree-ring cellulose.
Figure 5
Temporal correlation between the analysis and the truth for (a–d) temperature and (e–h) precipitation, for each experiment. The green dot represents the location of the proxy sampling site. The hatched area indicates where the correlation is not statistically significant ($p > 0.05$).
Figure 6

Temporal correlation between the analysis and the truth for each experiment for 1970–1999. The values for temperature and precipitation are the global mean of the temporal correlations.
Figure 7  
Temporal correlations between the analysis and the truth for (a–d) temperature and (e–h) precipitation, for (a and e) CTRL and (b–d and f–h) T2-Assim. The green dot represents the location of the proxy sampling site. The hatched area means that the correlation is not statistically significant ($p > 0.05$).
Figure 8: Temporal correlation between the analysis and the truth for each experiment for 1970–1999. The values for temperature and precipitation are the global mean of the temporal correlations.
Figure 9
Temporal correlations in North America between the analysis and the truth for (a–d) temperature, and (e–h) precipitation, for experiments using different proxy networks. The green dot represents the location of the proxy sampling site. The hatched area indicates where the correlation is not statistically significant ($p > 0.05$).